Blockchain technology and Bitcoin

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• list of records

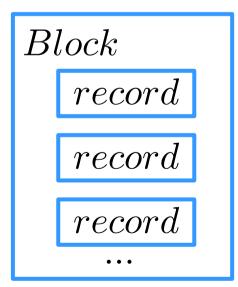
record

record

record



- list of records
- grouped in blocks





- list of records
- grouped in blocks
- linked in a chain

ledger

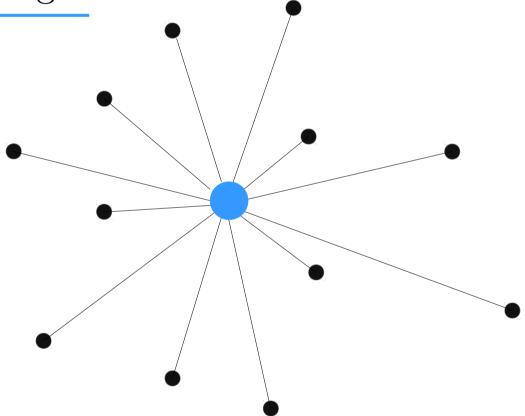
- add to chain
- can't modify old blocks

 $egin{array}{c} Block \\ record \\ record \\ \cdots \end{array}$

 $Block \\ record \\ record \\ record \\ \cdots$



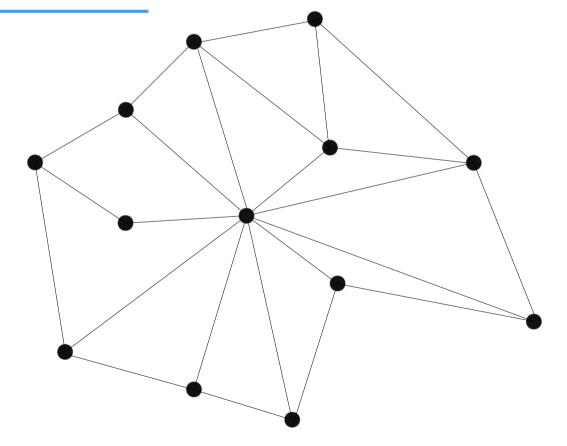
Centralized Ledger





Decentralized Ledger

Distributed



reduce, track down errors, corruption...



Public Blockchain: Bitcoin 😥

'Original Blockchain'

- cryptocurrency
 - → blockchain keeps track of wealth
- open source (Ex. Litecoin)
- trustless
- secured by miners
- whitepaper: bitcoin.org/bitcoin.pdf





Public Blockchain: Bitcoin 🥵

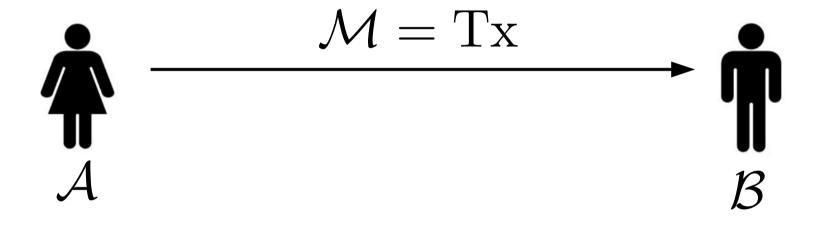
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- cryptocurrency
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Bitcoin Transactions (3)



How do you prove Alice sent the Message to \mathcal{B} ob?

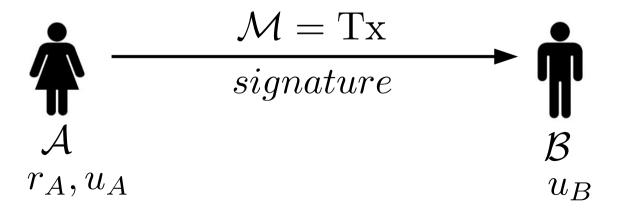


Bitcoin Transactions (3)

Cryptographic Signature

Signature

- public and private key pair generated $sig: r_A, \mathcal{M} \rightarrow signature$
- only A knows private key, r_A
- public key, u_A , known by everyone

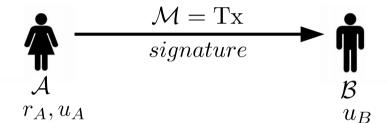




Bitcoin Transactions 😕

Cryptographic Signature

- public and private keys generated
- only A knows private key, r_A
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Verification

 $check: u_A, \mathcal{M}, signature \rightarrow Yes/No$

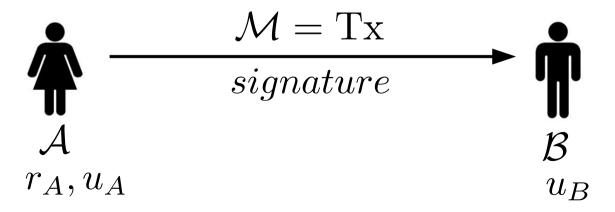
The \mathcal{M} essage can be verified by \mathcal{B} ob or anyone else



Bitcoin Transactions 😕

Overview

- participants in the network identified by public keys
 - \rightarrow \sim anonymity
- access to private key means access to funds
 - \rightarrow \sim access to 'wallet'
- transaction broadcasted and added to the ledger





Bitcoin Mining (3)

No central authority

Who keeps track of which transactions are valid?
double spending?
why?



Bitcoin Mining 🥵

Cryptographic Hash Function (H)

• maps any input to fixed size output

H(a) = ca978112ca1bbdcafac231b39a23dc4da786eff8147c4e72b9807785afee48bb

H("Bible") = 47f63b8cd8470051acd3a3c0bd5c77c4aa9574d79cf5bfb3e576facabbc11491



Bitcoin Mining (3)

Cryptographic Hash Function (H)

- maps any input to fixed size output
- not invertible



Bitcoin Mining 😕

Cryptographic Hash Function (H)

- maps any input to fixed size output
- not invertible
- not 'continuous'

```
\begin{split} H(\text{bank}) &= 4381 \text{dc} 2\text{ab} 14285160 \text{c} 808659 \text{aee} 005 \text{d} 51255 \text{add} 7264 \text{b} 318 \text{d} 07 \text{c} 7417292 \text{c} 7442 \text{c} \\ H(\text{Bank}) &= 676 \text{c} 471 \text{bc} 8 \text{dc} 3 \text{d} 1324133 \text{c} f 087 \text{c} 20 \text{aa} 0137 \text{fc} 02348811 \text{e} 4162 \text{c} 79 \text{e} 560298 \text{fb} 11 \\ H(\text{the bank}) &= \text{b3} \text{d} 0 \text{b} 18 \text{e} 01647 \text{cc} 301 \text{a} 5 \text{d} \text{c} 022784 \text{fd} 1 \text{e} 5 \text{b} 85475 \text{a} 4 \text{d} \text{b} \text{b} 14140 \text{b} 983 \text{d} \text{b} f 1 \text{c} 5 \text{a} 7 \text{b} \text{e} 1 \\ H(\text{thebank}) &= \text{fc} 4 \text{c} \text{b} 9 \text{f} 881175 \text{d} 7 \text{b} 5 \text{ac} 02906947 \text{f} 288 \text{b} 9998 \text{b} \text{d} 9354 \text{e} a06 \text{d} \text{d} f 13 \text{fc} 21 \text{fa} 5 \text{c} 12 \text{c} 4 \text{d} \\ \end{split}
```



Bitcoin Mining 😕

Cryptographic Hash Function (H)

- maps any input to fixed size output
- not invertible
- not 'continuous'
- no collisions

$$x \neq y \implies H(x) \neq H(y)$$



Bitcoin Mining (3)

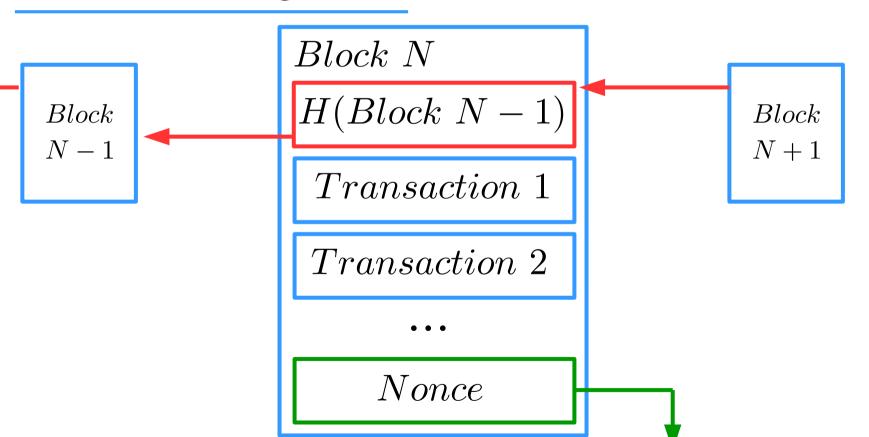
How does mining work?

- anyone in the network can add block
- hash of the block must start with a certain number of 0's
 - → determined by a difficulty parameter
 - \rightarrow H(Block) = 00000....ab142a1...
- blocks contain:
 - → hash of last block
 - → valid transactions





How does mining work?



picked so hash has correct amount of

Bitcoin Mining 🕖

What if someone cheats?

Block N-1

 $H(Block\ N-1)$

Transaction 1

Transaction 2

• • •

Nonce

Block N

 $H(Block\ N-1)$

Transaction 1

Transaction 2

Nonce

Block

N+1



Bitcoin Mining 🕖

What if someone cheats?

 $Block\ N-1$

H(Block N-2)

Transaction 1

Different Tx

• • •

Nonce



 $H(Block\ N-1)$

Transaction 1

Transaction 2

Nonce

Error gets propagated



Block

N+1

Bitcoin Mining 🥵

Overview

- miners add 1 MB blocks respecting current difficulty
- network accept valid blocks by adding blocks on the chain
 - → add blocks to <u>longest</u> valid chain (most work)
- blocks can only be added not modified
- new block is added every 10 minutes (on average)
 - → difficulty readjusted every 2 weeks
- miners are rewarded for adding blocks
 - → current reward: 12.5 BTC + fees
 - → first transaction in the block
 - \rightarrow total number of bitcoins is capped (~ 21 million coins)



Bitcoin Mining 🤔

Consumption

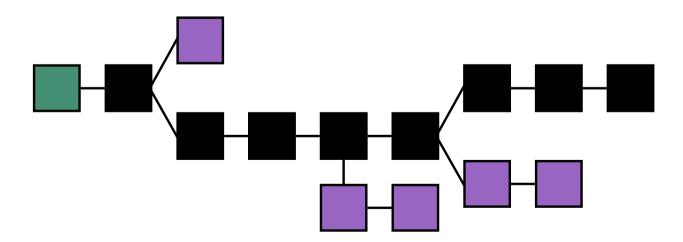
- in the beginning, mining could be done on a PC
- now, there are 'BTC mining farms'
- hashing electricity consumption
 - → 0.09% of world's power
 - → as much electricity as Syria
 - → enough to power 1,740,000 US households
 - \rightarrow 1 tx \sim powering 7 houses for a day
- Proposal for a fully decentralized blockchain and proof-of-work algorithm for solving NP-complete problems arXiv:1708.09419v2

source: https://digiconomist.net/bitcoin-energy-consumption

Bitcoin Mining (3)

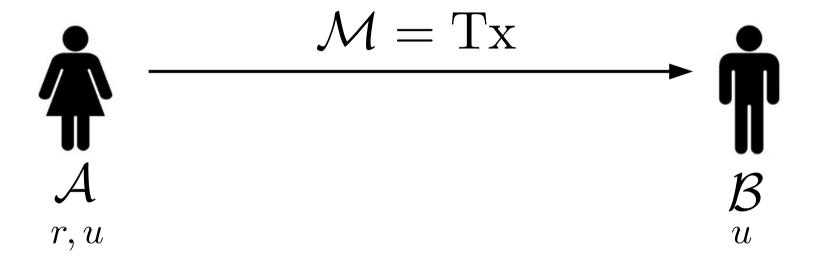
Longest Valid Chain

- longest chain will have the most valid transactions
- 51 % attack



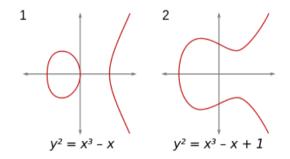


Bitcoin Transactions (3)



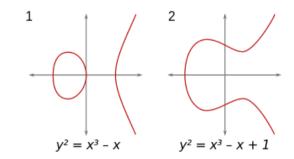


- public-key cryptography elliptic curves
- discrete-log problem





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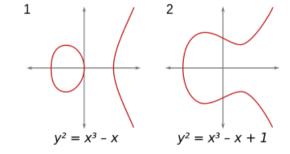


Find
$$k$$
, such that $b^k = a$

$$a, b \in G$$
 G is a group

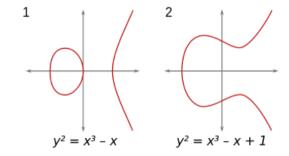


- public-key cryptography elliptic curves
- discrete-log problem
 - → Inefficient classically





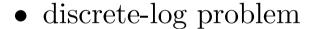
- public-key cryptography elliptic curves
- discrete-log problem
 - → Inefficient classically
- quantum computer: Shor's algorithm
 - → Efficient
- private key can be found from public key
 - → Funds are not secure



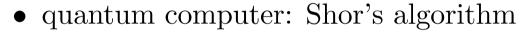


Transactions

• public-key cryptography - elliptic curves



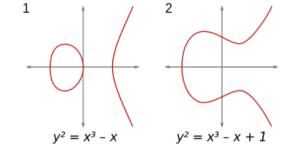
→ Inefficient classically



→ Efficient



- → Funds are not secure
- a lot of the encrypted communication breaks
 - → ways to fix this





Mining

• Classically: trial and error

$$\longrightarrow O(2^d)$$

• Quantum: Grover's Algorithm

$$\longrightarrow O(2^{d/2})$$

• better at mining than the rest of the network

$$\rightarrow d \sim 60$$

- eventually everyone has a quantum computer
 - → difficulty readjusted



Forking and Bitcoin Cash



Disagreement about the future

- issue: not enough transactions/block
 - ► scaling problem
- Bitcoin: segwit
 - restructure blocks
- Bitcoin Cash: Larger blocks

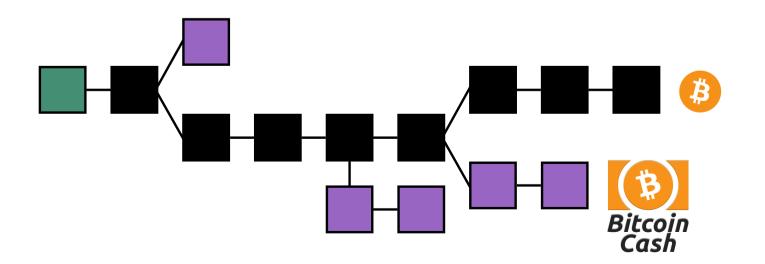


Forking and Bitcoin Cash



Resolution of the conflict

- fork the ledger
- same past, different future
- different miners agree to work on different chains



1 MB blocks

8 MB blocks

Other Ideas

Cryptocurrencies

- Bitcoin is first, is it best?
- Ethereum: smart contracts
- Iota: tangle
- Quantum Resistant Ledger: 'resistant' to quantum computers









Other Ideas

Smart Contracts

- decentralized applications dApps
- Ex. Pear: decentralized journal
 - → https://github.com/ricott1/Pear





